



Overview Small Steps

Equivalent fractions

- Improper fractions to mixed numbers
- Mixed numbers to improper fractions
- Number sequences
- Compare and order fractions less than 1
- Compare and order fractions greater than 1
- Add and subtract fractions
- Add fractions within 1
- Add 3 or more fractions
- Add fractions
- Add mixed numbers
- Subtract fractions
- Subtract mixed numbers
- Subtract breaking the whole

NC Objectives

Compare and order fractions whose denominators are multiples of the same number.

Identify, name and write equivalent fractions of a given fraction, represented visually including tenths and hundredths.

Recognise mixed numbers and improper fractions and convert from one form to the other and write mathematical statements >1 as a mixed number [for example $\frac{2}{5} + \frac{4}{5} = \frac{6}{5} = 1\frac{1}{5}$]

Add and subtract fractions with the same denominator and denominators that are multiples of the same number.



Overview Small Steps

- Multiply unit fractions by an integer
- Multiply non-unit fractions by an integer
- Multiply mixed numbers by integers
- Fraction of an amount
- Using fractions as operators

NC Objectives

Multiply proper fractions and mixed numbers by whole numbers, supported by materials and diagrams.

Read and write decimal numbers as fractions [for example $0.71 = \frac{71}{100}$]

Solve problems involving multiplication and division, including scaling by simple fractions and problems involving simple rates.



Equivalent Fractions

Notes and Guidance

Children explore equivalent fractions using models and concrete representations.

They use models to make the link to multiplication and division. Children then apply the abstract method to find equivalent fractions.

It is important children have the conceptual understanding before moving on to just using an abstract method.

Mathematical Talk

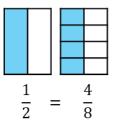
What equivalent fractions can we find by folding the paper? How can we record these?

What is the same and what is different about the numerators and denominators in the equivalent fractions?

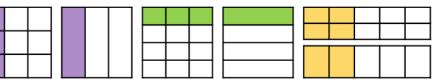
How does multiplication and division help us find equivalent fractions? Where can we see this in our model?

Varied Fluency

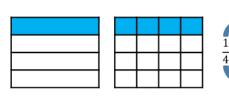
Take two pieces of paper the same size. Fold one piece into two equal pieces. Fold the other into eight equal pieces. What equivalent fractions can you find?



Use the models to write equivalent fractions.

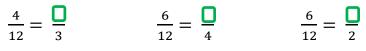


Eva uses the models and her multiplication and division skills to find equivalent fractions.



Use this method to find equivalent fractions to $\frac{2}{4}, \frac{3}{4}$ and $\frac{4}{4}$ where the denominator is 16

Eva uses the same approach to find equivalent fractions for these fractions. How will her method change?





Equivalent Fractions

Reasoning and Problem Solving

Rosie says,

To find equivalent fractions, whatever you do to the numerator, you do to the denominator.

Using her method, here are the equivalent fractions Rosie has found for $\frac{4}{8}$

$\frac{4}{8} =$	8 16	$\frac{4}{8} =$	$\frac{6}{10}$
$\frac{4}{8} =$	$\frac{2}{4}$	$\frac{4}{8} =$	$\frac{1}{5}$

Are all Rosie's fractions equivalent? Does Rosie's method work? Explain your reasons.

$\frac{4}{8} =$	$\frac{1}{5}a$	nd $\frac{4}{8} =$	6 10
are	inco	rrect.	

Rosie's method doesn't always work. It works when multiplying or dividing both the numerator or denominator but not when adding or subtracting the same thing to both.

Ron thinks you can only simplify even numbered fractions because you keep on halving the numerator and denominator until you get an odd number. Do you agree? Explain your answer.	Ron is wrong. For example $\frac{3}{9}$ can be simplified to $\frac{1}{3}$ and these are all odd numbers.
Here are some fraction cards.	A = 10
All of the fractions are equivalent.	B = 6
$\begin{array}{c} \hline 4\\ \hline A \end{array} \qquad \hline B\\ \hline C \end{array} \qquad \hline 20\\ \hline 50\\ \hline 50\\ \end{array}$ $A + B = 16\\ Calculate the value of C. \end{array}$	C = 15



Improper to Mixed Numbers

Notes and Guidance

Children convert improper fractions to mixed numbers for the first time. An improper fraction is a fraction where the numerator is greater than the denominator. A mixed number is a number consisting of an integer and a proper fraction.

It is important for children to see this process represented visually to allow them to make the connections between the concept and what happens in the abstract.

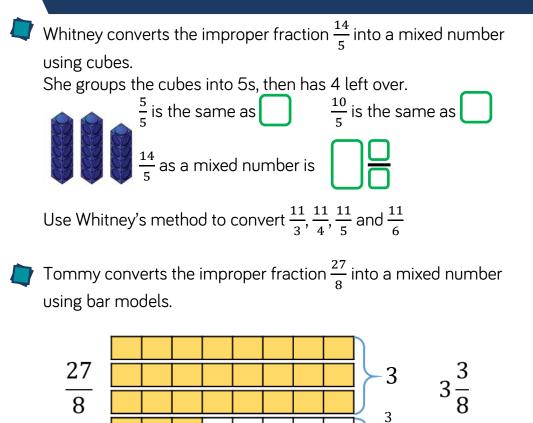
Mathematical Talk

How many parts are there in a whole?

What do you notice happens to the mixed number when the denominator increases and the numerator remains the same?

What happens when the numerator is a multiple of the denominator?

Varied Fluency

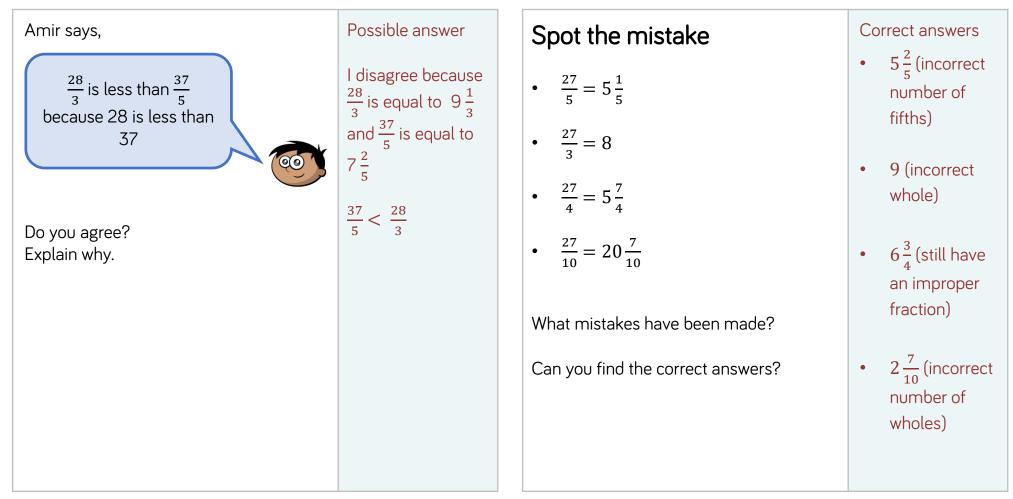


Use Tommy's method to convert $\frac{25}{8}$, $\frac{27}{6}$, $\frac{18}{7}$ and $\frac{32}{4}$



Improper to Mixed Numbers

Reasoning and Problem Solving





Mixed Numbers to Improper

Notes and Guidance

Children now convert from mixed numbers to improper fractions using concrete and pictorial methods to understand the abstract method.

Ensure children always write their working alongside the concrete and pictorial representations so they can see the clear links to the abstract.

Mathematical Talk

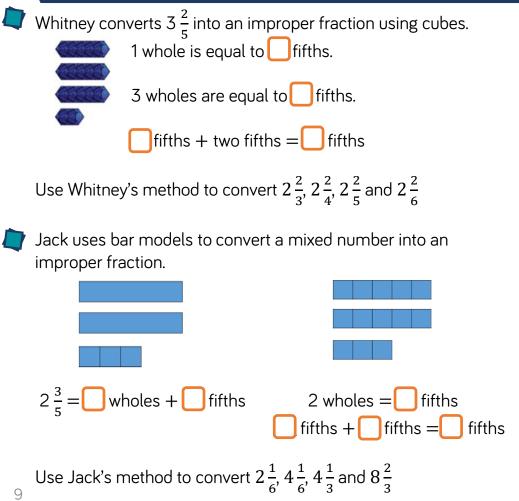
How many quarters/halves/eighths/fifths are there in a whole?

How does multiplication support us in converting from mixed numbers to improper fractions?

Can you explain the steps in converting an improper fraction to a mixed number? Use the vocabulary: numerator, denominator, multiply, add

How could we use the previous bar model to help?

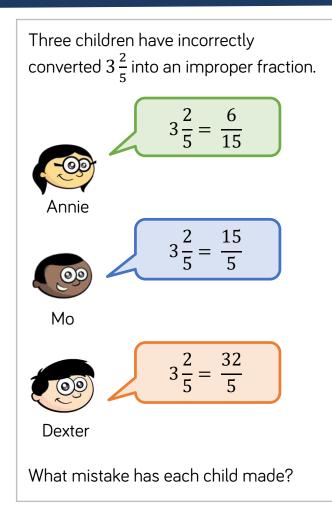
Varied Fluency





Mixed Numbers to Improper

Reasoning and Problem Solving

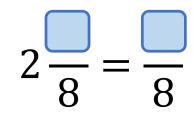


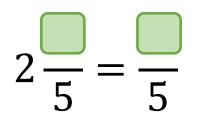
Annie has multiplied the numerator and denominator by 3

Mo has multiplied the correctly but then forgotten to add on the extra 2 parts.

Dexter has just placed 3 in front of the numerator. Fill in the missing numbers.

How many different possibilities can you find for each equation?





Compare the number of possibilities you found.

 $2\frac{1}{8} = \frac{17}{8} \qquad 2\frac{2}{8} = \frac{18}{8}$ $2\frac{3}{8} = \frac{19}{8} \qquad 2\frac{4}{8} = \frac{20}{8}$ $2\frac{5}{8} = \frac{21}{8} \qquad 2\frac{6}{8} = \frac{22}{8}$ $2\frac{7}{8} = \frac{23}{8}$

There will be 4 solutions for fifths.

Teacher notes: Encourage children to make generalisations that the number of solutions is one less than the denominator.



Number Sequences

Notes and Guidance

Children count up and down in a given fraction. They continue to use visual representations to help them explore number sequences.

Children also find missing fractions in a sequence and determine whether the sequence is increasing or decreasing and by how much.

Mathematical Talk

What are the intervals between the fractions?

Are the fractions increasing or decreasing? How much are they increasing or decreasing by?

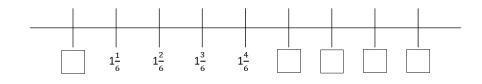
Can you convert the mixed numbers to improper fractions? Does this make it easier to continue the sequence?

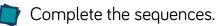
Varied Fluency

Use the counting stick to count up and down in these fractions.

- Start at 0 and count up in steps of $\frac{1}{4}$
- Start at 4 and count down in steps of $\frac{1}{3}$
- Start at 1 and count up in steps of $\frac{2}{3}$

Complete the missing values on the number line.





- $\frac{3}{4}, \frac{1}{2}, 1\frac{3}{4}, 2\frac{1}{4}$
- $\frac{1}{2}$, 5 $\frac{1}{2}$, 5 $\frac{7}{10}$, 5 $\frac{9}{10}$

 $\frac{1}{2}, 3\frac{1}{3}, \frac{1}{2}, 2\frac{2}{3}$ $\frac{3}{5}, \frac{1}{2}, \frac{1}{2}, \frac{1}{2}, 3$



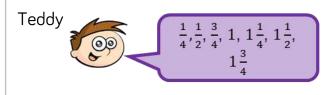
Number Sequences

Reasoning and Problem Solving

Three children are counting in quarters.





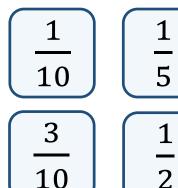


Eva $\frac{1}{4}, \frac{2}{4}, \frac{3}{4}, 1, 1\frac{1}{4}, 1\frac{2}{4}, \frac{3}{4}, \frac{1}{4}, \frac{3}{4}, \frac{3}{4}, \frac{1}{4}, \frac{3}{4}, \frac{3}{4},$

Who is counting correctly? Explain your reasons.

They are all correct, they are all counting in quarter. Teddy has simplified all answers and Eva has converted improper fractions to mixed numbers. Play the fraction game for four players. Place the four fraction cards on the floor. Each player stands in front of a fraction. We are going to count up in tenths starting at O

When you say a fraction, place your foot on your fraction.



How can we make 4 tenths? What is the highest fraction we can count to? How about if we used two feet? Children can make four tenths by stepping on one tenth and three tenths at the same time. With one foot, they can count up to 11 tenths or one and one tenth. With two feet they can count up to 22 tenths



Compare & Order (Less than 1)

Notes and Guidance

Children build on their equivalent fraction knowledge to compare and order fractions less than 1 where the denominators are multiples of the same number.

Children compare the fractions by finding a common denominator or a common numerator. They use bar models to support their understanding.

Mathematical Talk

How does a bar model help us to visualise the fractions?

Should both of our bars be the same size? Why? What does this show us?

If the numerators are the same, how can we compare our fractions?

If the denominators are the same, how can we compare our fractions?

Do we always have to find a common denominator? Can we find a common numerator?

Varied Fluency

	Use bar models to compare $\frac{5}{8}$ and $\frac{3}{4}$	
		□ > □
		□ < □
	Use this method to help you compare: $\frac{5}{6}$ and $\frac{2}{3}$ $\frac{2}{3}$ and $\frac{5}{9}$ $\frac{7}{16}$ and $\frac{3}{8}$	
	Use common numerators to help you co	mpare $\frac{2}{5}$ and $\frac{2}{3}$
		□ > □
s		□ < □
5	Use this method to help you compare: $\frac{6}{7}$ and $\frac{6}{8}$ $\frac{4}{9}$ and $\frac{4}{5}$ $\frac{4}{11}$ and $\frac{2}{5}$	
	Order the fractions from greatest to small $\frac{3}{7}, \frac{3}{5}$ and $\frac{3}{8}$ $\frac{2}{3}, \frac{5}{6}$ and $\frac{7}{12}$ $\frac{6}{11}, \frac{3}{5}$	allest: and $\frac{2}{3}$



Compare & Order (Less than 1)

Reasoning and Problem Solving

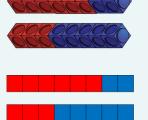
Ron makes $\frac{3}{4}$ and $\frac{3}{8}$ out of cubes.





He thinks that $\frac{3}{8}$ is equal to $\frac{3}{4}$

Do you agree? Explain your answer. Possible answer: I disagree with Ron because the two wholes are not equal. He could have compared using numerators or converted $\frac{3}{4}$ to $\frac{6}{8}$ If he does this he will see that $\frac{3}{4}$ is greater. Children may use bar models or cubes to show this.



Always, sometimes, never?

If one denominator is a multiple of the other you can simplify the fraction with the larger denominator to make the denominators the same.

Example:

Could
$$\frac{?}{4}$$
 and $\frac{?}{12}$ be simplified to $\frac{?}{4}$ and $\frac{?}{4}$?

Prove it.

Sometimes

It does not work for some fractions e.g. $\frac{8}{15}$ and $\frac{3}{5}$ But does work for

others e.g. $\frac{1}{4}$ and $\frac{9}{12}$



Compare & Order (More than 1)

Notes and Guidance

Children use their knowledge of ordering fractions less than 1 to help them compare and order fractions greater than 1

They use their knowledge of common denominators to help them.

Children will compare both improper fractions and mixed numbers during this step.

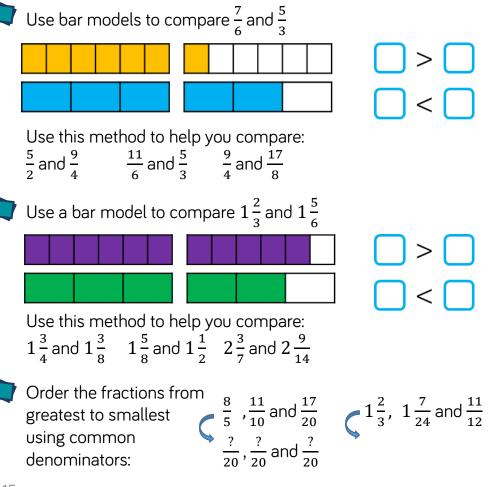
Mathematical Talk

How can we represent the fractions?

- How does the bar help us see which fraction is the greatest?
- Can we use our knowledge of multiples to help us?
- Can you predict which fractions will be greatest? Explain how you know.

Is it more efficient to compare using numerators or denominators?

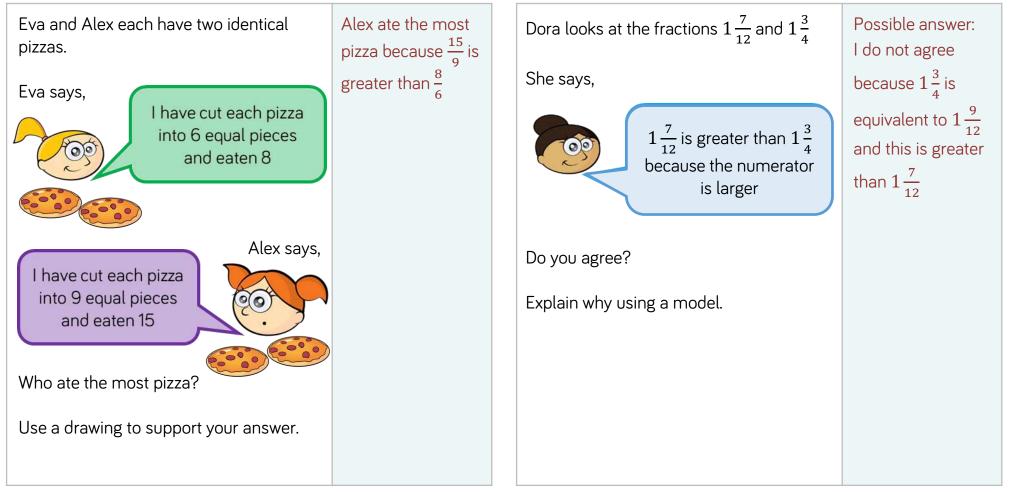
Varied Fluency





Compare & Order (More than 1)

Reasoning and Problem Solving





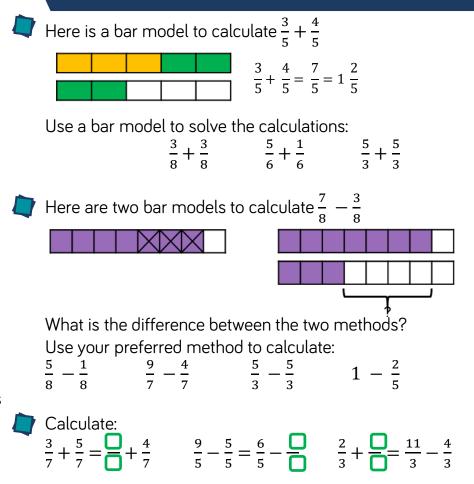
Add & Subtract Fractions

Notes and Guidance

Children recap their Year 4 understanding of adding and subtracting fractions with the same denominator.

They use bar models to support understanding of adding and subtracting fractions.

Varied Fluency



Mathematical Talk

- How many equal parts do I need to split my bar into?
- Can you convert the improper fraction into a mixed number?

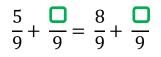
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How can a bar model help you balance both sides of the equals sign?
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Add & Subtract Fractions

Reasoning and Problem Solving

How many different ways can you balance the equation?



Possible answers:				
$\frac{5}{9} + \frac{3}{9} = \frac{8}{9} + \frac{0}{9}$				
$\frac{5}{9} + \frac{4}{9} = \frac{8}{9} + \frac{1}{9}$				
$\frac{5}{9} + \frac{5}{9} = \frac{8}{9} + \frac{2}{9}$				
Any combination of fractions where the numerators				

Any combination of fractions where the numerators add up to the same total on each side of the equals sign.

A chocolate bar has 12 equal pieces.	Amir eats $\frac{8}{12}$ of the
Amir eats $\frac{5}{12}$ more of the bar than Whitney.	chocolate bar and Whitney eats $\frac{3}{12}$ of the chocolate bar.
There is one twelfth of the bar remaining.	
What fraction of the bar does Amir eat?	
What fraction of the bar does Whitney eat?	



Add Fractions within 1

Notes and Guidance

Children add fractions with different denominators for the first time where one denominator is a multiple of the other.

They use pictorial representations to convert the fractions so they have the same denominator.

Ensure children always write their working alongside the pictorial representations so they see the clear links.

Mathematical Talk

Can you find a common denominator? Do you need to convert both fractions or just one?

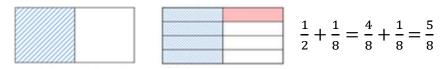
Can you explain Mo and Rosie's methods to a partner? Which method do you prefer?

How do Mo and Rosie's methods support finding a common denominator?

Varied Fluency

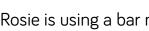
Mo is calculating $\frac{1}{2} + \frac{1}{8}$

He uses a diagram to represent the sum.



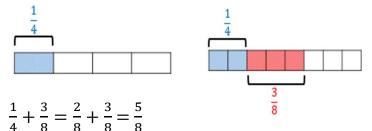
Use Mo's method to solve :

1 3	1 3	7 1
$\frac{-}{2} + \frac{-}{8}$	$\frac{-}{4} + \frac{-}{8}$	$\frac{10}{10} + \frac{1}{5}$



$$r = har model to solve $\frac{1}{r}$$$

Rosie is using a bar model to solve $\frac{1}{4} + \frac{3}{8}$



Use a bar model to solve:

 $\frac{1}{6} + \frac{5}{12}$ $\frac{2}{9} + \frac{1}{3}$ $\frac{1}{3} + \frac{4}{15}$



Add Fractions within 1

Reasoning and Problem Solving

$\frac{5}{16} + \frac{15}{8} = \frac{15}{16}$ $\frac{1}{20} + \frac{7}{10} = \frac{17}{20}$	5 3
Annie solved this calculation.	Annie is wrong because she has just added the numerators and the denominators. When adding fractions with different denominators you need to find a common denominator.
Can you spot and explain her mistakes	

Two children are solving $\frac{1}{3} + \frac{4}{15}$

Eva starts by drawing this model:

Alex starts by drawing this model:



Can you explain each person's method and how they would complete the question? Which method do you prefer and why?

Possible answer: Each child may have started with a different fraction in the calculation. e.g. Eva has started by shading a third. She now needs to divide each third into five equal parts so there are fifteen equal parts altogether. Eva will then shade $\frac{4}{15}$ and will have $\frac{9}{15}$ altogether.



Add 3 or More Fractions

Notes and Guidance

Children add more than 2 fractions where two denominators are a multiple of the other.

They use a bar model to continue exploring this.

Ensure children always write their working alongside the pictorial representations so they see the clear links.

Mathematical Talk

Can you find a common denominator? Do you need to convert both fractions or just one?

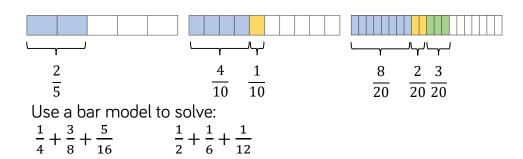
Can you explain Ron's method to a partner? How does Ron's method support finding a common denominator?

Can you draw what Farmer Staneff's field could look like? What fractions could you divide your field into?

Why would a bar model not be efficient for this question?

Varied Fluency

Ron uses a bar model to calculate $\frac{2}{5} + \frac{1}{10} + \frac{3}{20}$



Farmer Staneff owns a field. He plants carrots on $\frac{1}{3}$ of the field. He plants potatoes on $\frac{2}{9}$ of the field. He plants onions on $\frac{5}{18}$ of the field. What fraction of the field is covered altogether?

Complete the fractions.

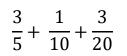


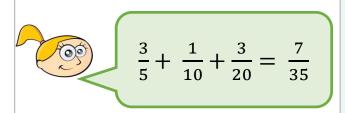


Add 3 or More Fractions

Reasoning and Problem Solving

Eva is attempting to answer:





Do you agree with Eva? Explain why. Eva is wrong because she has added the numerators and denominators together and hasn't found a common denominator. The correct answer is $\frac{17}{20}$

Jack has added 3 fractions together to get an answer of $\frac{17}{18}$	Possible answers: $\frac{1}{18} + \frac{4}{18} + \frac{13}{18}$
	$\overline{18}^+ \overline{18}^+ \overline{18}^+$ $\frac{1}{9} + \frac{5}{9} + \frac{5}{18}$
What 3 fractions could he have added?	$\frac{1}{9} + \frac{1}{9} + \frac{1}{18}$
Can you find more than one answer?	$\frac{1}{6} + \frac{5}{9} + \frac{2}{9}$
	$\frac{1}{18} + \frac{1}{6} + \frac{13}{18}$
	$\frac{1}{3} + \frac{1}{6} + \frac{4}{9}$



Add Fractions

Notes and Guidance

Children continue to represent adding fractions using pictorial methods to explore adding two or more proper fractions where the total is greater than 1

Children can record their totals as an improper fraction but will then convert this to a mixed number using their prior knowledge.

Mathematical Talk

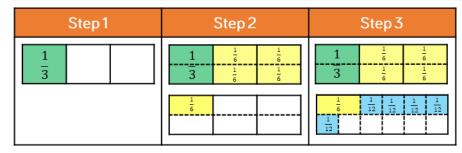
How does the pictorial method support me to add the fractions?

Which common denominator will we use?

How do my times-tables support me to add fractions?

Which representation do you prefer? Why?

Varied Fluency



$$\frac{1}{3} + \frac{5}{6} + \frac{5}{12} = 1\frac{7}{12}$$

Explain each step of the calculation.

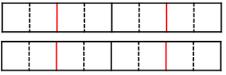
Use this method to help you add the fractions.

Give your answer as a mixed number.

2 	$\frac{1}{-}+$	7	<u>1</u> _	<u>7</u> _	3	<u>1</u> _	<u>5</u> _	5
3		12	4	8	16	2	6	12

Use the bar model to add the fractions. Record your answer as a mixed number.

$$\frac{3}{4} + \frac{3}{8} + \frac{1}{2} =$$



Draw your own models to solve:

$$\frac{5}{12} + \frac{1}{6} + \frac{1}{2} \qquad \frac{11}{20} + \frac{3}{5} + \frac{1}{10} \qquad \frac{3}{4} + \frac{5}{12} + \frac{1}{22}$$



Add Fractions

Reasoning and Problem Solving

Annie is adding three fractions. She uses the model to help her.



What could her three fractions be?

How many different combinations can you find?

Can you write a number story to represent your calculation?

Possible answer:

 $\frac{2}{3} + \frac{4}{12} + \frac{1}{2} = 1\frac{1}{2}$

Other equivalent fractions may be used.

Example story: Some children are eating pizzas. Jack eats two thirds, Amir eats four twelfths and Dexter eats half a pizza. How much pizza did they eat altogether? The sum of three fractions is $2\frac{1}{8}$

The fractions have different denominators.

All of the fractions are greater than or equal to a half.

None of the fractions are improper fractions.

All of the denominators are factors of 8

What could the fractions be?

 $\frac{1}{2} + \frac{3}{4} + \frac{7}{8}$

Children could be given less clues and explore other possible solutions.



Add Mixed Numbers

Notes and Guidance

Children move on to adding two fractions where one or both are mixed numbers or improper fractions.

They will use a method of adding the wholes and then adding the parts. Children will record their answer in its simplest form.

Children can still draw models to represent adding fractions.

Mathematical Talk

How can we partition these mixed numbers into whole numbers and fractions?

What will the wholes total? Can I add the fractions straight away?

What will these mixed numbers be as improper fractions?

If I have an improper fraction in the question, should I change it to a mixed number first? Why?

Varied Fluency

$$1\frac{1}{3} + 2\frac{1}{6} = 3 + \frac{3}{6} = 3\frac{3}{6} \text{ or } 3\frac{1}{2}$$

Add the fractions by adding the whole first and then the fractions. Give your answer in its simplest form.

$$1 + 2 = 3$$

$$\frac{1}{3} + \frac{1}{6} = \frac{2}{6} + \frac{1}{6} = \frac{3}{6}$$

 $3\frac{1}{4} + 2\frac{3}{8} \qquad 4\frac{1}{9} + 3\frac{2}{3} \qquad 2\frac{5}{12} + 2\frac{1}{3}$

$$1\frac{3}{4} + 2\frac{1}{8} = \frac{7}{4} + \frac{17}{8} = \frac{14}{8} + \frac{17}{8} = \frac{31}{8} = 3\frac{7}{8}$$

Add the fractions by converting them to improper fractions.

$$1\frac{1}{4} + 2\frac{5}{12} \qquad 2\frac{1}{9} + 1\frac{1}{3} \qquad 2\frac{1}{6} + 2\frac{2}{3}$$

Add these fractions.

$4\frac{7}{9}+2\frac{1}{3}$	$\frac{17}{1} + 1\frac{1}{1}$	$\frac{15}{1} + 2\frac{1}{1}$
9 3	6 3	8 4

How do they differ from previous examples?



Add Mixed Numbers

Reasoning and Problem Solving

Jack and Whitney have some juice.

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Jack drinks 2\frac{1}{4} litres and Whitney drinks 2\frac{5}{12} litres.
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How much do they drink altogether?

Complete this using two different methods.

Which method do you think is more efficient? Why?



Encourage children to justify which method they prefer and why. Ensure children discuss which method is more or less efficient.

4

$$\frac{5}{6}$$
 + = 10 $\frac{1}{3}$

$$5\frac{3}{6} \text{ or } 5\frac{1}{2}$$

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Subtract Fractions

Notes and Guidance

Children subtract fractions with different denominators for the first time, where one denominator is a multiple of the other.

It is important that subtraction is explored as both take away and finding the difference.

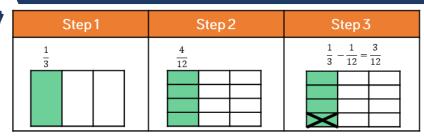
Mathematical Talk

What could the common denominator be?

Can you draw a model to help you solve the problem?

Is it easier to use a take away bar model (single bar model) or a bar model to find the difference (comparison model)?

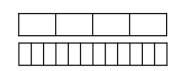
Varied Fluency



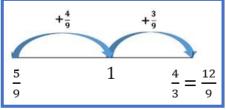
Explain each step of the calculation.

Use this method to help you solve $\frac{5}{6} - \frac{1}{3}$ and $\frac{7}{8} - \frac{5}{16}$

- Tommy and Teddy both have the same sized chocolate bar. Tommy has $\frac{3}{4}$ left, Teddy has $\frac{5}{12}$ left. How much more does Tommy have?



Amir uses a number line to find the difference between $\frac{5}{9}$ and $\frac{4}{3}$



4 3

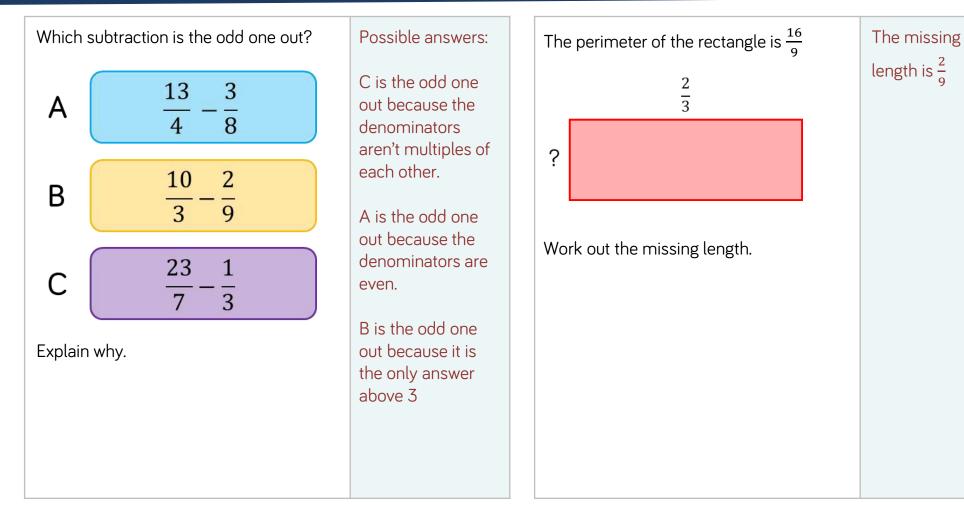
Use this method to find the difference between:

030 0113 11100100		
$\frac{3}{4}$ and $\frac{5}{4}$	$\frac{19}{15}$ and $\frac{3}{5}$	$\frac{20}{-}$ and
– and —	— and –	— and
4 12	15 5	9



Subtract Fractions

Reasoning and Problem Solving





Subtract Mixed Numbers (1)

Notes and Guidance

Children apply their understanding of subtracting fractions where one denominator is a multiple of the other to subtract proper fractions from mixed numbers.

They continue to use models and number lines to support their understanding.

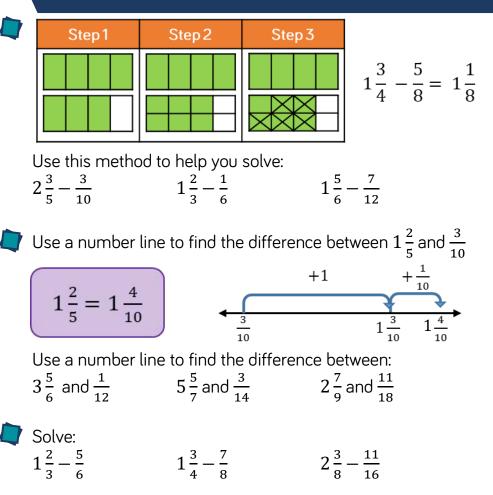
Mathematical Talk

- Which fraction is the greatest? How do you know?
- If the denominators are different, what can we do?

Can you simplify your answer?

Which method do you prefer when subtracting fractions: taking away or finding the difference?

Varied Fluency





Subtract Mixed Numbers (1)

Reasoning and Problem Solving

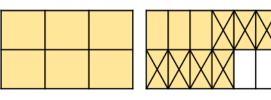
Amir is attempting to solve $2\frac{5}{14} - \frac{2}{7}$

Here is his working out:

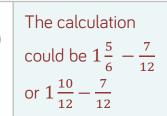
$$2\frac{5}{14} - \frac{2}{7} = 2\frac{3}{7}$$

Do you agree with Amir? Explain your answer. Possible answer:

Amir is wrong because he hasn't found a common denominator when subtracting the fractions he has just subtracted the numerators and the denominators. The correct answer is $2\frac{1}{14}$ Here is Rosie's method. What is the calculation?



Can you find more than one answer? Why is there more than one answer?



There is more than one answer because five sixths and ten twelfths are equivalent. Children should be encouraged to write the question as $1\frac{5}{6} - \frac{7}{12}$ so that all fractions are in their simplest form.



Subtract Mixed Numbers (2)

Notes and Guidance

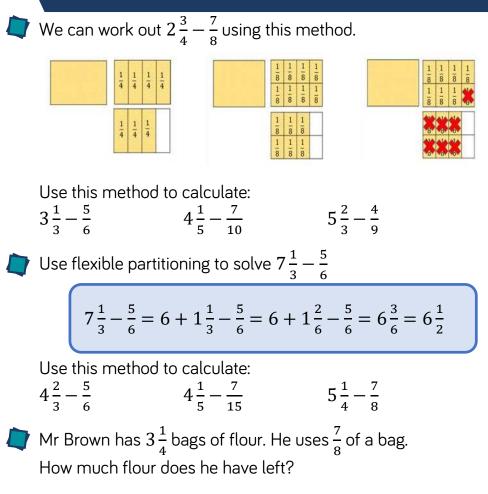
Children use prior knowledge of fractions to subtract two fractions where one is a mixed number and you need to break one of the wholes up.

They use the method of flexible partitioning to create a new mixed number so they can complete the calculation.

Mathematical Talk

- Is flexible partitioning easier than converting the mixed number to an improper fraction?
- Do we always have to partition the mixed number?
- When can we subtract a fraction without partitioning the mixed number in a different way?

Varied Fluency





Subtract Mixed Numbers (2)

Reasoning and Problem Solving

Place 2, 3 and 4 in the boxes to make the calculation correct.

$$27\frac{1}{0} - \frac{1}{6} = 26\frac{1}{3}$$

$$27\frac{1}{2} - \frac{4}{6} = 26\frac{2}{2}$$

3 children are working out $6\frac{2}{3} - \frac{5}{6}$

They partition the mixed number in the following ways to help them.

Dora
$$5 + 1\frac{2}{3} - \frac{5}{6}$$

Alex $5 + 1\frac{4}{6} - \frac{5}{6}$
Jack $5 + \frac{10}{6} - \frac{5}{6}$

Are they all correct? Which method do you prefer? Explain why. All three children are correct.

 $1\frac{2}{3}$, $1\frac{4}{6}$ and $\frac{10}{6}$ are all equivalent therefore all three methods will help children to correctly calculate the answer.



Subtract 2 Mixed Numbers

Notes and Guidance

Children use different strategies to subtract two mixed numbers.

Building on learning in previous steps, they look at partitioning the mixed numbers into wholes and parts and build on their understanding of flexible partitioning as well as converting to improper fractions when an exchange is involved.

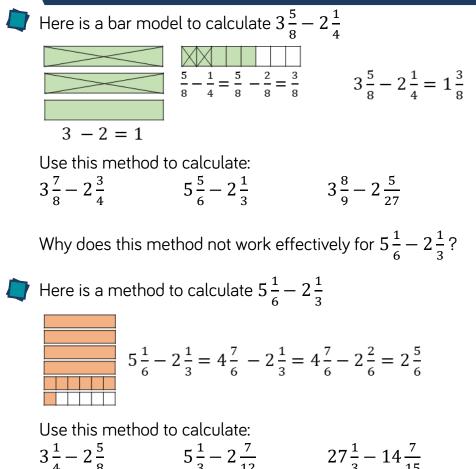
Mathematical Talk

Why is subtracting the wholes and parts separately easier with some fractions than others?

Can you show the subtraction as a difference on a number line? Bar model? How are these different to taking away?

Does making the whole numbers larger make the subtraction any more difficult? Explain why.

Varied Fluency





Subtract 2 Mixed Numbers

Reasoning and Problem Solving

There are three colours of dog biscuits in a bag of dog food: red, brown and orange. The total mass of the dog food is 7 kg. The mass of red biscuits is $3\frac{3}{4}$ kg and the	$3\frac{3}{4} + 1\frac{7}{16} = 5\frac{3}{16}$ 7 - 5\frac{3}{16} = 1\frac{13}{16} The mass of orange biscuits is	Rosie has 20 $\frac{3}{4}$ cm of ribbon. Annie has 6 $\frac{7}{8}$ cm less ribbon than Rosie. How much ribbon does Annie have?	Annie has $13\frac{7}{8}$ cm of ribbon. Altogether they have $34\frac{5}{8}$ cm of ribbon
mass of the brown biscuits is $1\frac{7}{16}$ kg. What is the mass of orange biscuits?	1 13 kg.	How much ribbon do they have altogether?	ribbon.



4 sixths

Multiply by an Integer (1)

Notes and Guidance

Children are introduced to multiplying fractions by a whole number for the first time. They link this to repeated addition and see that the denominator remains the same, whilst the numerator is multiplied by the integer.

This is shown clearly through the range of models to build the children's conceptual understanding of multiplying fractions. Children should be encouraged to simplify fractions where possible.

Mathematical Talk

How is multiplying fractions similar to adding fractions?

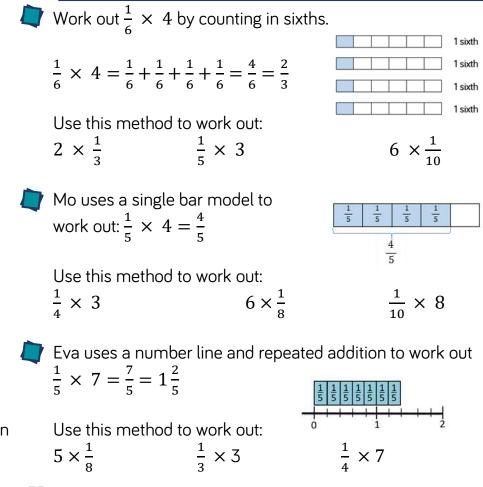
What is the same/different between: $\frac{3}{4} \times 2$ and $2 \times \frac{3}{4}$?

Which bar model do you find the most useful?

Which bar model helps us to convert from an improper fraction to a mixed number most effectively?

What has happened to the numerator/denominator?

Varied Fluency



35



Multiply by an Integer (1)

Reasoning and Problem Solving

Amir is multiplying fractions by a whole number.

 $\frac{1}{5} \times 5 = \frac{5}{25}$

Can you explain his mistake?

Always, sometimes, never?

When you multiply a unit fraction by the same number as it's denominator the answer will be one whole.

Amir has multiplied both the numerator and the denominator so he has found an equivalent fraction. Encourage children to draw models to represent this correctly. Always - because the numerator was 1 it will always be the same as your

denominator when

e.g. $\frac{1}{3} \times 3 = \frac{3}{3} = 1$

multiplied which means that it is a

whole.

I am thinking of a unit fraction.	$\frac{1}{8}$
When I multiply it by 4 it will be equivalent to $\frac{1}{2}$	4 ar
2	2
When I multiply it by 2 it will be equivalent to $\frac{1}{4}$	
What is my fraction?	
What do I need to multiply my fraction	6
by so that my answer is equivalent to $\frac{3}{4}$?	6
Can you create your own version of this problem?	

 $\frac{1}{3} \text{ because}$ $4 \times \frac{1}{8} = \frac{4}{8} = \frac{1}{2}$ and $2 \times \frac{1}{8} = \frac{2}{8} = \frac{1}{4}$ 6 because $6 \times \frac{1}{8} = \frac{6}{8} = \frac{3}{4}$



Multiply by an Integer (2)

Notes and Guidance

Children apply prior knowledge of multiplying a unit fraction by a whole number to multiplying a non-unit fraction by a whole number.

They use similar models and discuss which method will be the most efficient depending on the questions asked. Reinforce the concept of commutativity by showing examples of the fraction first and the integer first in the multiplication.

Mathematical Talk

Can you show me 3 lots of $\frac{3}{10}$ on a bar model?

How many tenths do we have altogether?

How does repeated addition help us with this multiplication?

How does a number line help us see the multiplication?

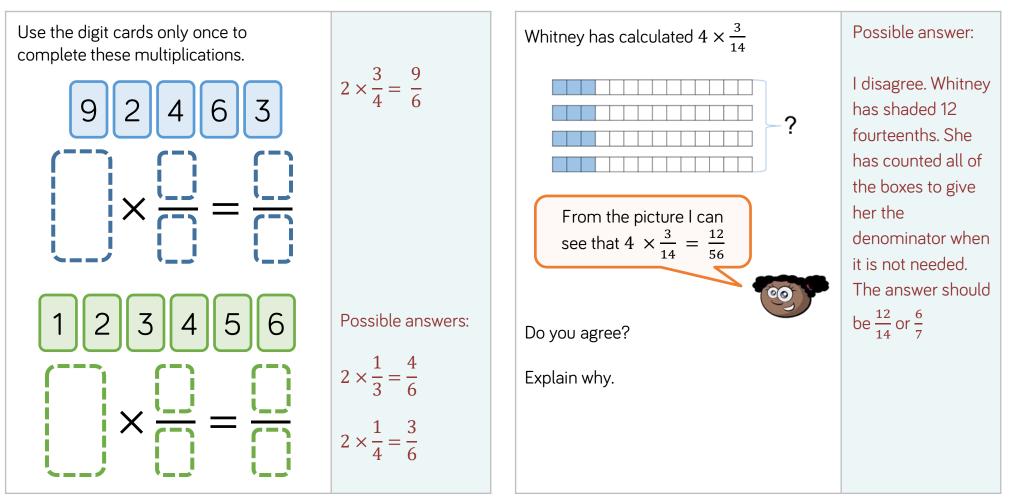
Varied Fluency

Count the number	r of ninths to wor	$k 3 \times \frac{2}{9}$		
$\frac{1}{9}$ $\frac{1}{9}$		Ĩ		
$\frac{1}{9}$ $\frac{1}{9}$				
$\frac{1}{9}$ $\frac{1}{9}$				
Use this method to				
$\frac{3}{8} \times 2$	$\frac{5}{16} \times 3$	$4 \times \frac{2}{11}$		
Use the model to	help you solve 3	$\times \frac{2}{10}$		
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	$\begin{array}{c ccccccccccccccccccccccccccccccccccc$			
$\frac{2}{7} \times 3$	$\frac{3}{16} \times 4$	$4 \times \frac{5}{12}$		
Use the number li	ne to help			
you solve $2 \times \frac{3}{7}$		3 7	3 7	-
Use this method to		$\frac{1}{7}$ $\frac{1}{7}$ $\frac{1}{7}$ $\frac{1}{7}$ $\frac{1}{7}$	$\frac{4}{7}$ $\frac{5}{7}$ $\frac{6}{7}$ $\frac{7}{7}$ $\frac{7}{7}$	777
$\frac{3}{10} \times 3$	$\frac{2}{7} \times 2$	$4 \times \frac{3}{20}$		



Multiply by an Integer (2)

Reasoning and Problem Solving





Multiply by an Integer (3)

Notes and Guidance

Children use their knowledge of fractions to multiply a mixed number by a whole number.

They use the method of repeated addition, multiplying the whole and part separately and the method of converting to an improper fraction then multiplying.

Continue to explore visual representations such as the bar model.

Mathematical Talk

How could you represent this mixed number?

What is the denominator? How do you know?

How many wholes are there? How many parts are there?

What is multiplying fractions similar to? (repeated addition)

What representation could you use to convert a mixed number to an improper fraction?

Varied Fluency

Use repeated addition to work out $2\frac{2}{3} \times 4$

$$2\frac{2}{3} \times 4 = 2\frac{2}{3} + 2\frac{2}{3} + 2\frac{2}{3} + 2\frac{2}{3} + 2\frac{2}{3} = 8\frac{8}{3} = 10\frac{2}{3}$$

Use this method to solve:

$$2\frac{1}{6} \times 3$$
 $1\frac{3}{7} \times 2$ $3\frac{1}{3} \times 4$

Partition your fraction to help you solve $2\frac{3}{4} \times 3$

$$2 \times 3 = 6$$

$$\frac{3}{4} \times 3 = \frac{9}{4} = 2\frac{1}{4}$$

$$6 + 2\frac{1}{4} = 8\frac{1}{4}$$

Use this method to answer:

$$2\frac{5}{6} \times 3$$
 $3\frac{4}{7} \times 2$ $2\frac{1}{3} \times 5$

 $1\frac{5}{6} \times 3 = \frac{11}{6} \times 3 = \frac{33}{6} = 5\frac{3}{6} = 5\frac{1}{2}$

```
Convert to an improper fraction to calculate:

3\frac{2}{7} \times 4 2\frac{4}{9} \times 2 4 \times 3\frac{3}{5}
```



Multiply by an Integer (3)

Reasoning and Problem Solving

Jack runs $2\frac{2}{3}$ × Jack runs $2\frac{2}{2}$ miles three times per week. Work out the missing numbers. Possible answer: $2\frac{5}{8} \times 3 = 7\frac{7}{8}$ 3 = 8 miles. Dexter runs $3\frac{3}{4}$ miles twice a week. Dexter runs I knew that the $3\frac{3}{4} \times 2 = 7\frac{1}{2}$ Who runs the furthest during the week? multiplier could miles. not be 4 because Explain your answer. that would give an Jack runs further Explain how you worked it out. answer of at least by half a mile. 8. So the multiplier had to be 3. That meant that the missing numerator had to give a product of 15. I knew that 5 multiplied by 3 would give 15



Fraction of an Amount

Notes and Guidance

Children recap previous learning surrounding finding unit and non-unit fractions of amounts, quantities and measures.

It is important that the concept is explored pictorially through bar models to support children to make sense of the abstract.

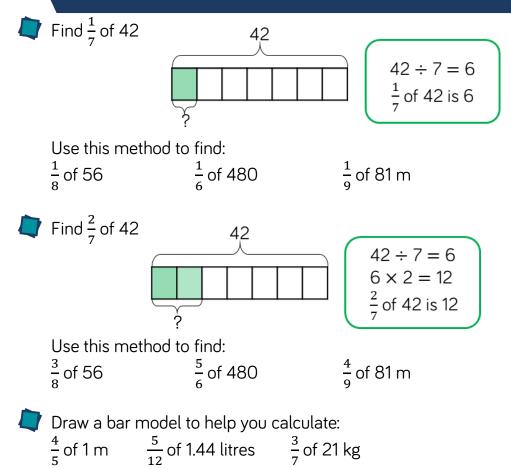
Mathematical Talk

How many equal groups have you shared 49 into? Why?

What does each equal part represent as a fraction and an amount?

What could you do to 1 metre to make the calculation easier?

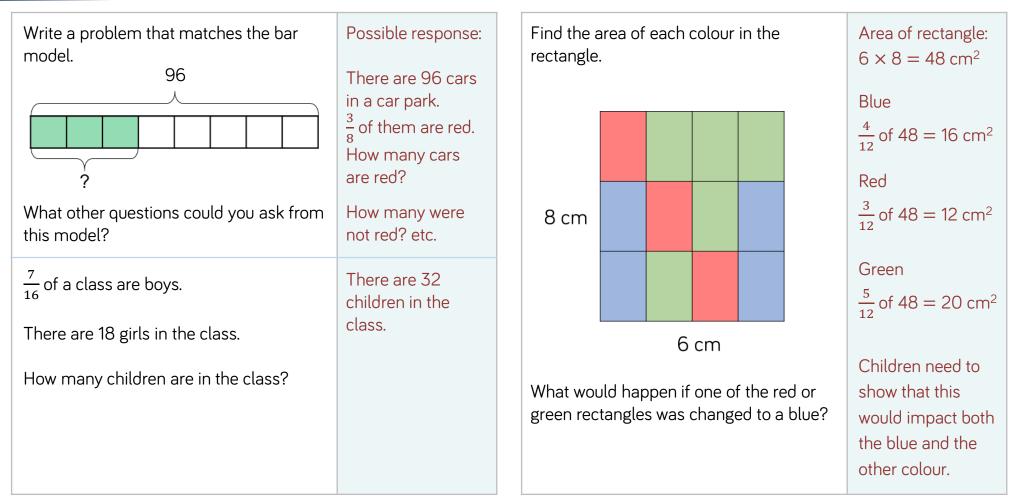
Varied Fluency





Fraction of an Amount

Reasoning and Problem Solving





Fractions as Operators

Notes and Guidance

Children link their understanding of fractions of amounts and multiplying fractions to use fractions as operators.

They use their knowledge of commutativity to help them understand that you can change the order of multiplication without changing the product.

Varied Fluency

Tommy has calculated and drawn a bar model for two calculations.

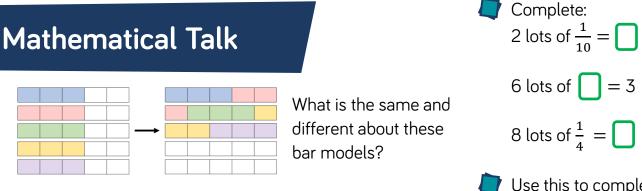


 $\frac{1}{10}$ of 2 =

 $\frac{1}{4}$ of 8 =

of 6 = 3

What's the same and what's different about Tommy's calculations?



Which calculation on each row is easier? Why?

 $x^{\frac{2}{3}} = 0$ of 18 = 12

Is it easier to multiply a fraction or find a fraction of an amount? Does it depend on the whole number you are multiplying by? Can you see the link between the numbers? Use this to complete:

$$20 \times \frac{4}{5} = 0$$
 of $20 = 0$

$$x \frac{1}{3} = \frac{1}{3} \text{ of } = 20$$



Fractions as Operators

Reasoning and Problem Solving

Which method would you use to complete these calculations: multiply the fractions or find the fraction of an amount?

Explain your choice for each one. Compare your method to your partner.

$$25 \times \frac{3}{5} \text{ or } \frac{3}{5} \text{ of } 25$$
$$6 \times \frac{2}{3} \text{ or } \frac{2}{3} \text{ of } 6$$
$$5 \times \frac{3}{8} \text{ or } \frac{3}{8} \text{ of } 5$$

Possible response:

- Children may find it easier to find 3 fifths of 25 rather than multiply 25 by 3
 Children may choose either as they are of similar efficiency.
- Children will probably find it more efficient to multiply than divide 5 by 8

	Dexter and Jack are thinking of a two- digit number between 20 and 30	They started with 24
	Dexter finds two thirds of the number. Jack multiplies the number by $\frac{2}{3}$	Dexter: 24 \div 3 = 8 8 × 2 = 16
	Their new two-digit number has a digit total that is one more than that of their original number. What number did they start with?	Jack: 24 \times 2 = 48 48 \div 3 = 16
	Show each step of their calculation.	